

Number – addition and subtraction

Number – multiplication and division

add numbers mentally, including:

- a three-digit number and ones
- a three-digit number and tens
- a three-digit number and hundreds

Counting on $115 + 2$ "Put 115 in your head, 116, 117."	Adding near numbers and adjusting $433 + 90 = 433 + 100 - 10$ $= 533 - 10$ $= 523$
Partition number and recombine $127 + 90 = 100 + 20 + 7 + 90$ $= 100 + 110 + 7$ $= 100 + 117$ $= 217$	Count on by splitting units to make next multiple of ten/hundred $360 + 80 = 360 + 40 + 40$ $= 400 + 40$ $= 440$

- two two-digit numbers (including answer crossing 100)

Counting on with number lines $48 + 36 = 84$ 	Partition both numbers and recombine $27 + 82 = 20 + 7 + 80 + 2$ $= 100 + 9$ $= 109$
Add the nearest multiple of 10, then adjust $63 + 59$ is the same as $63 + 60 - 1$	Count on by partitioning the second number only $36 + 93 = 36 + 30 + 6$ $= 123 + 6$ $= 129$

subtract numbers mentally, including:

- a three-digit number and ones
- a three-digit number and tens
- a three-digit number and hundreds

Counting back: $263 - 5$ "Put 263 in your head, 262, 261, 260, 259, 258."	Use unprepared numbered lines to subtract, by counting back: $516 - 400 = 116$
Subtract mentally a 'near multiple of 10' to or from a two-digit number: $678 - 90 = 678 - 100 + 10$	$116 - 400 = 116$

- two two-digit numbers (including answer crossing 100)

Find a small difference by counting up $42 - 39 = 3$ 	Subtract mentally a number near 10 to or from a two-digit number $35 - 19 = 35 - 20 + 1$
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recall and use multiplication facts for the 3, 4 and 8 multiplication tables

Play games, chant, test etc to increase speed of recalling facts. Make models and images to display facts.
Investigate patterns within tables.

recall and use division facts for the 3, 4 and 8 multiplication tables

Play games, chant, test etc to increase speed of recalling facts. Make models and images to display facts.
Investigate patterns within tables.

understand and use mental methods using commutativity and associativity (for example, $4 \times 12 \times 5 = 4 \times 5 \times 12 = 20 \times 12 = 240$)

Use a variety of resources (including a calculator) to investigate order of multiplication.
Make models and images to display facts.

understand and use mental methods using multiplication facts (e.g. using $3 \times 2 = 6$, $6 \div 3 = 2$ and $2 = 6 \div 3$) to derive related facts (e.g. $30 \times 2 = 60$, $60 \div 3 = 20$ and $20 = 60 \div 3$)

$30 \times 5 = 150$	$50 \times 3 = 150$	$150 \div 5 = 30$	$150 \div 3 = 50$
$3 \times 5 = 15$	$5 \times 3 = 15$	$15 \div 3 = 5$	
$3 \times 50 = 150$	$5 \times 30 = 150$	$150 \div 30 = 5$	
$5 \times 30 = 150$	$50 \times 30 = 1500$	$30 \times 50 = 1500$	$150 \div 50 = 3$

add numbers with up to three digits, using formal written methods of columnar addition (See Appendix 1)

We begin by teaching the partitioned column method with carrying (using dienes as support)

$$\begin{array}{r} 200 + 40 + 6 \\ 70 + 6 \\ \hline 300 + 20 + 2 \\ 100 \quad 10 \end{array}$$

Extend mental method of partitioning and recombining. $158 + 72 = 100 + (50 + 70) + (8 + 2)$ $= 100 + 120 + 10$ $= 230$	Vertical expansion 367 $+185$ 12 140 400 552
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Column addition Including Money

367 $+ 185$ $\hline 552$	$\pounds 2.50$ $+ \pounds 1.75$ $\hline \pounds 4.25$
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Use base 10 (dienes) or place value counters to support understanding of carrying and to ensure conceptual understanding of place value:

subtract numbers with up to three digits, using formal written methods of columnar subtraction (See Appendix 1)

Use base 10 (dienes) as a practical method to introduce exchanging

$$31 - 18 = 13$$

When pupil(s) are confident in doing this practically and verbalizing the calculation, begin to record using partitioned column method:

$20 \quad 1$ $30 + 1$ $-10 + 8$ $\hline 10 + 3$	When secure with exchanging, use partitioned column method to solve calculations involving 3 digit numbers. Repeating the practical stage if necessary.
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Introduce Column Subtraction without decomposition:

$$\begin{array}{r} 458 \\ - 232 \\ \hline 226 \end{array}$$

develop reliable written methods for multiplication, starting with calculations of two-digit numbers by one-digit numbers and progressing to the formal written methods of short multiplication

Start by reinforcing mental methods of partitioning:

$15 \times 2 = 30$ 	$13 \times 3 = (10 \times 3) + (3 \times 3)$ $= 30 + 9$ $= 39$
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Grid Method

1. Introduce the grid method by linking it to arrays initially (using counters):
2. Use base 10 (dienes) with grid method to support understanding of place value:
3. Use the grid method:

$12 \times 3 = 36$ 	$12 \times 3 = 36$ 	$12 \times 3 = 36$
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develop reliable written methods for division, starting with calculations of two-digit numbers by one-digit numbers and progressing to the formal written methods of short division

Use counters and a number line to support pupils understanding, Number lines
How many 3's make 18?

Hoops and dots
 $16 \div 2 = 8$

Move on to calculations that leave remainders and/or require tables knowledge:

1) $16 \div 3 = 5 \text{ r } 1$

2) $69 \div 3 = 23$

When pupils have had experience with and demonstrated understanding of grouping for division, begin to look at short division with no remainders in the final answer.

Use counters/Dienes to support understanding.

$3 \overline{) 96}$	
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Number – addition and subtraction

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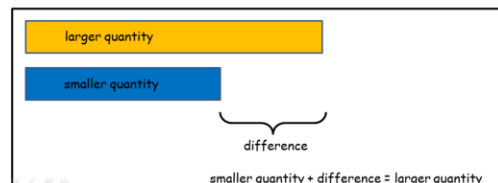
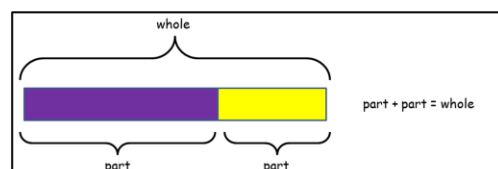
solve problems, including missing number problems, using number facts, place value, and more complex addition

Missing numbers should be placed in all possible places:

$$\begin{array}{rcl} 3 + 4 & = & 4 + 3 \\ 3 + & = & 7 \quad 7 = +4 \\ 4 + & = & 7 \quad 7 = 3 + \\ + \nabla & = & 7 \quad 7 = + \nabla \end{array}$$

Use all the models and images mentioned above.
Discuss which is most effective and why.

Singapore Bar Method



estimate the answer to a calculation and use inverse operations to check answers

Estimate answers before solving any calculation.
Once inverse operation has been learnt use as a method for checking.

use a variety of language to describe addition

+, add, addition, more, plus, make, sum, total, altogether, score, double, near double, one more, two more... ten more... one hundred more, how many more to make...? how many more is... than...? how much more is...?

= equals, sign, is the same as

tens boundary, hundreds boundary

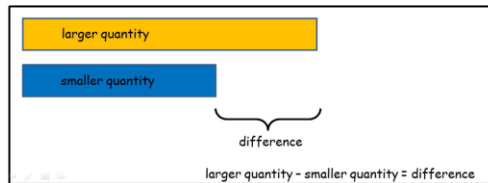
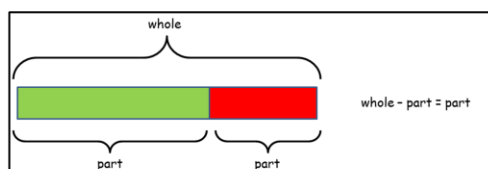
solve problems, including missing number problems, using number facts, place value, and more complex subtraction

Missing numbers should be placed in all possible places:

$$\begin{array}{rcl} 16 - 9 & = & 16 - 9 \\ 16 - & = & 7 \quad 7 = - 9 \\ - 9 & = & 7 \quad 7 = 16 - \\ - \nabla & = & 7 \quad 7 = - \nabla \end{array}$$

Use all the models and images mentioned above. Discuss which is most effective and why.

Singapore Bar Method



estimate the answer to a calculation and use inverse operations to check answers

Estimate answers before solving any calculation.
Once inverse operation has been learnt use as a method for checking.

use a variety of language to describe subtraction

- subtract, subtraction, take (away), minus, leave, how many are left/left over? one less, two less... ten less... one hundred less, how many fewer is... than...? how much less is...? difference between, half, halve

= equals, sign, is the same as

solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects

solve simple problems in contexts, deciding which of the four operations to use and why

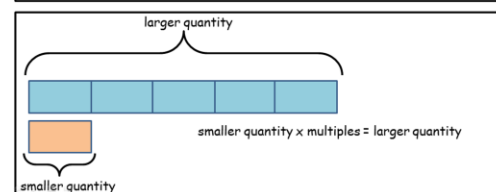
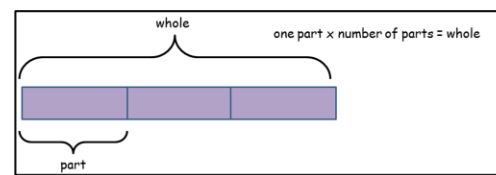
Missing numbers placed in all possible places.

$$\begin{array}{rcl} 7 \times 2 & = & 2 \times 7 \\ 7 \times & = & 14 \quad 14 = \times 7 \\ - \times 2 & = & 14 \quad 14 = 2 \times \\ - \times \nabla & = & 14 \quad 14 = \times \nabla \end{array}$$

Extend to
 $2 \times 6 = 3 \times$
and using three numbers
 $10 \times \times = 60 \quad 12 = 2 \times \times 2$

Use all the models and images mentioned above. Discuss which is most effective and why.

Singapore Bar Method



write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods

See models and images above.

use a variety of language to describe multiplication

count, count (up) to, count on (from, to), count back (from, to), count in ones, twos, threes, fours, fives... count in tens, hundreds, lots of, groups of, , times, multiply, multiplication, multiplied by, multiple of, product, once, twice, three times... ten times... times as (big, long, wide... and so on), repeated addition, array, row, column

= equals, sign, is the same as

solve problems, including missing number problems, involving division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects

solve simple problems in contexts, deciding which of the four operations to use and why

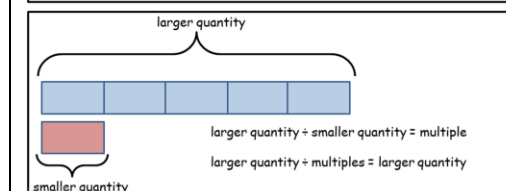
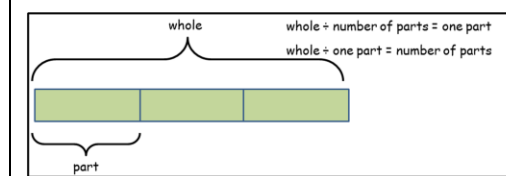
Missing numbers placed in all possible places.

$$\begin{array}{rcl} 6 \div 2 & = & 6 \div 2 \\ 6 \div & = & 3 \quad 3 = 6 \div \\ - \div 2 & = & 3 \quad 3 = \div 2 \\ - \div \nabla & = & 3 \quad 3 = \div \nabla \end{array}$$

Extend to
 $12 \div 6 = 8 \div$
and using three numbers
 $10 \div 5 \div = 1 \quad 3 = 12 \div \div 2$

Use all the models and images mentioned above. Discuss which is most effective and why.

Singapore Bar Method



write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods

See models and images above.

use a variety of language to describe division

Array, row, column, halve, share, share equally, one each, two each, three each... group in pairs, threes... tens, equal groups of, ÷, divide, division, divided by, divided into, left, left over, remainder

= equals, sign, is the same as