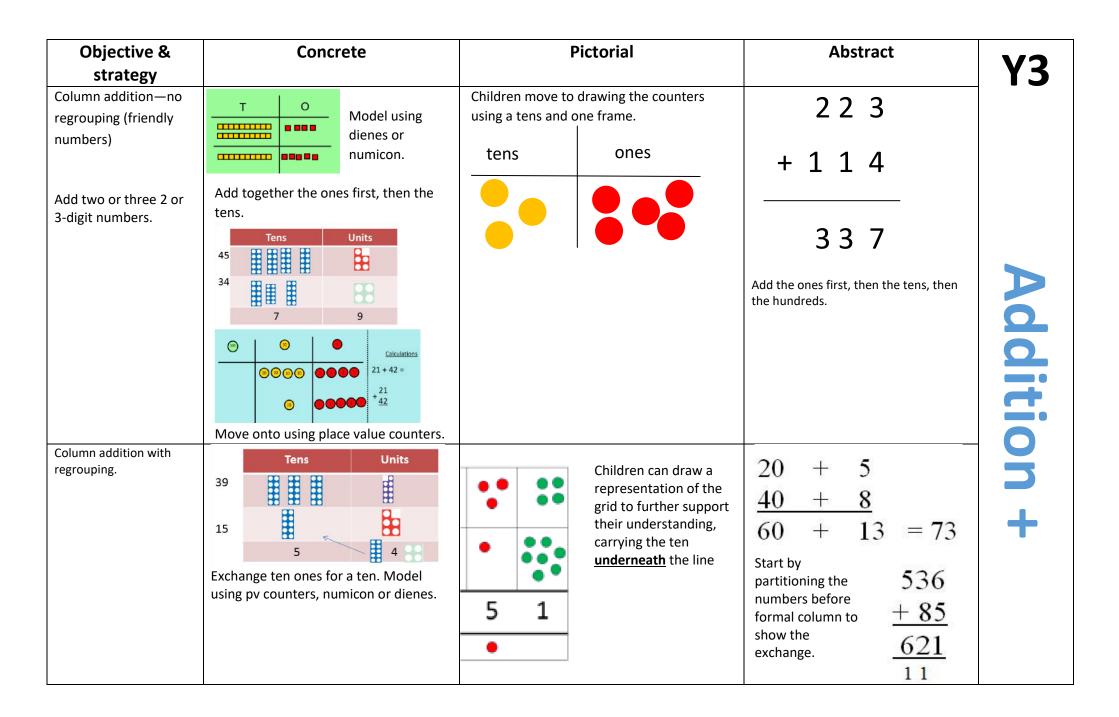


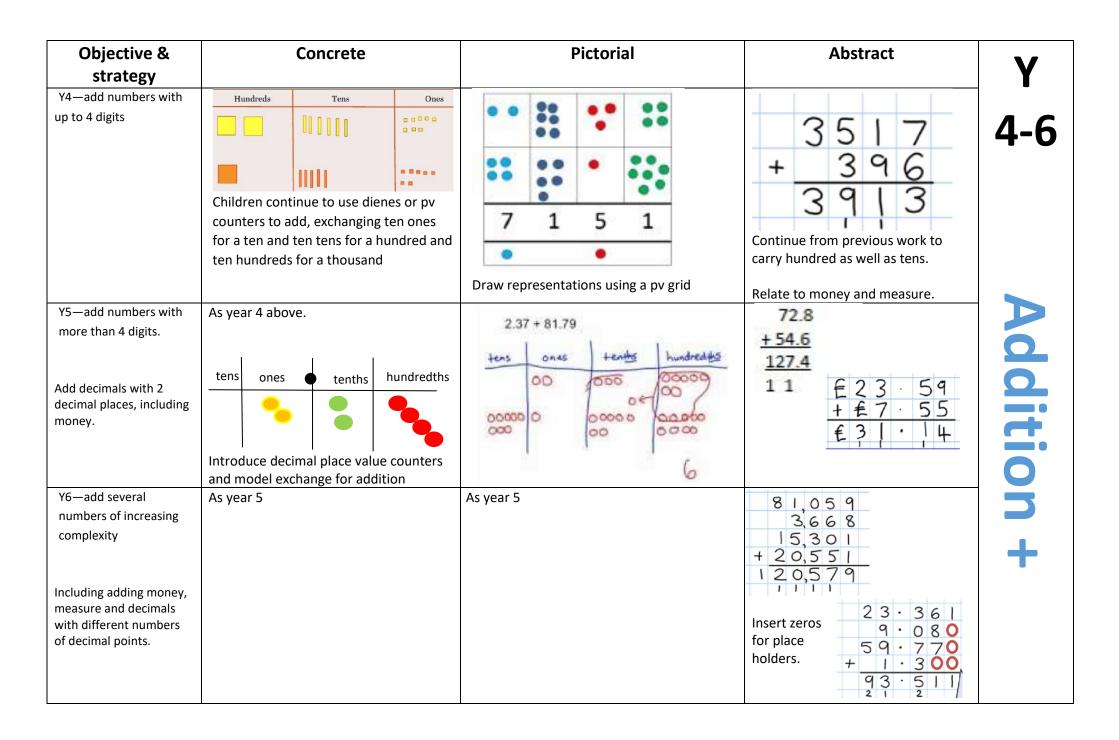


Calculation Policy

This policy has been largely adapted from the White Rose Maths Hub Calculation Policy with further material added. It is a working document and will be revised and amended as necessary.

Objective &	Concrete	Pictorial	Abstract	V1
strategy				ΥY
Combining two parts to make a whole:part- whole model	Use part part whole	yhole 2	4 + 3 = 7 10 10 = 6 + 4	
	Use cubes to add two numbers together as a group or in a bar	3 Balls 2 Balls	Use the part-part whole diagram to move into the abstract	
		Use pictures to add two numbers together as a group or in a bar.		
Starting at the bigger number and counting on	***************************************	12 + 5 10 11 12 13 14 15 16 17 18 19 20 = 17	5 + 12 = 17 Place the larger number in your head	9
Oll	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	Start at the larger number on the number line and count on in ones or in one jump to find the answer.	and count on the smaller number to find your answer.	dit
Regrouping to make 10 This is an essential skill for column addition later.	6+5=11	3 + 9 = Use pictures or a number line. Regroup or	7 + 4= 11 If I am at seven, how many more do I	Addition
	Start with the bigger number and use the smaller	partition the smaller number using the part part whole model to make 10. $9 + 5 = \boxed{14}$	need to make 10. How many more do I add on now?	+
	number to make 10. Use ten frames	0 1 2 3 4 5 6 7 8 9 (10) 11 12 13 (14) 15 16 17 18 19 20		
Represent & use number bonds and related subtraction	.3333) zezza)) vete	Draw 2 more hata	Emphasis should be on the language '1 more than 5 is equal to 6.' '2 more than 5 is 7.'	
facts within 20	2 more than 5.	5+2=	'8 is 3 more than 5.'	





Objective & strategy	Concrete	Pictorial	Abstract	Y1
Taking away ones	Use physical objects, counter, cubes etc to show how objects can be taken away. $6-4=2$	Cross out drawn objects to show what has been taken away.	7—4 = 3 16—9 = 7	-
	4-2=2	15-3= 12		SL
Counting back	080	5 - 3 = 2	Put 13 in your head, count back 4. What number are you at?	bt
	Move objects away from the group,	0 1 2 3 4 5 6 7 8 9 10		
	counting backwards.	Count back in ones using a number line.		oi
	Move the beads along the bead string as you count back.			Subtraction
Find the difference	Compare objects and amounts 7 'Seven is 3 more than four' 4 'I am 2 years older than my	Count on using a number line to find the difference.	Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister?	nc.
	. sister' 5 Pencils	+6		•
		0 1 2 3 4 5 6 7 8 9 10 11 12		
	3 Erasers ? Lay objects to represent bar model.			
	Lay objects to represent bar model.			

Objective & strategy	Concrete	Pictorial	Abstract	Y1
Represent and use number bonds and related subtraction facts within 20 Part Part Whole model	Link to addition. Use PPW model to model the inverse. If 10 is the whole and 6 is one of the parts, what is the other part? $10-6=4$	Use pictorial representation to show the part.	Move to using numbers within the part whole model.	Su
Make 10	14 – 9 Make 14 on the ten frame. Take 4 away to make ten, then take one more away so that you have taken 5.	13 – 7 = 6 -4 -3 -3 -4 -3 -3 -4 -3 -3 -13 – 7 Jump back 3 first, then another 4. Use ten as the stopping point.	16—8 How many do we take off first to get to 10? How many left to take off?	Subtraction
Bar model	5 -2 = 3		8 2 10 = 8 + 2 10 = 2 + 8 10 - 2 = 8 10 - 8 = 2	ion -

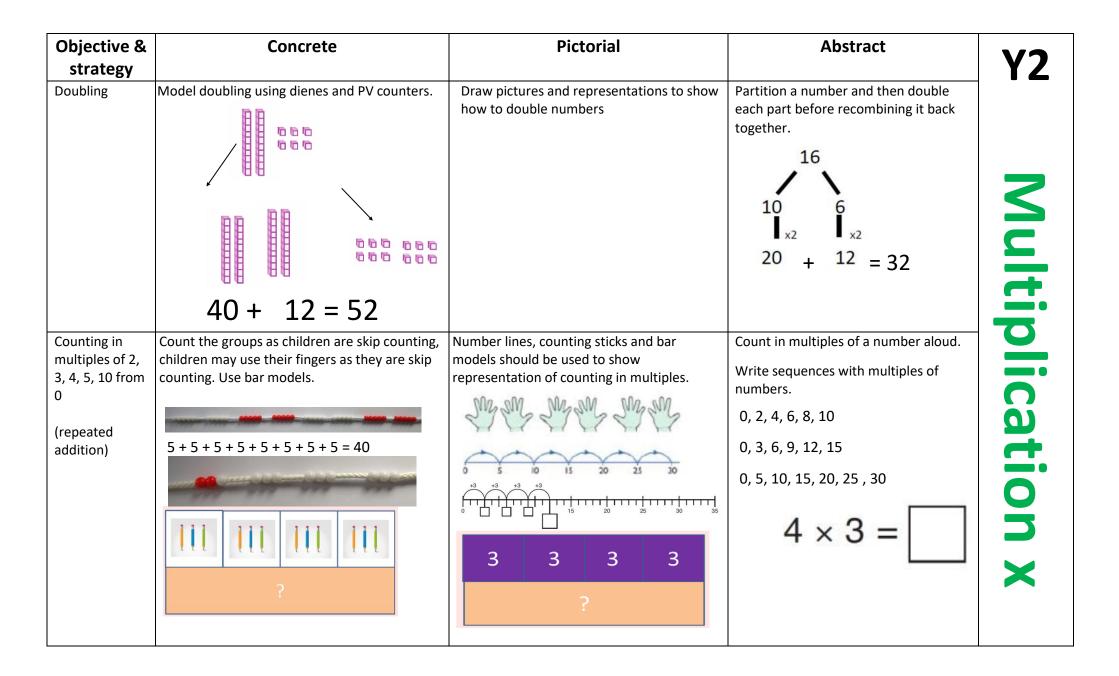
Objective & strategy	Concrete	Pictorial	Abstract	Y2
Regroup a ten into ten ones	Use a pv chart to show how to change a ten into ten ones, use the term 'take and make'	20 – 4 =	20—4 = 16	
Partitioning to subtract without regrouping. 'Friendly numbers'	Use dienes to show how to partition the number when subtracting without regrouping	Children draw representations of dienes and cross off. 43—21 = 22	43—21 = 22	Subtraction
Make ten strategy Progression should be crossing one ten, crossing more than one ten, crossing the hundreds	34—28 Use a bead bar or bead strings to model counting to next ten and the rest.	76 80 90 93 'counting on' to find 'difference' Use a number line to count on to next ten and then the rest.	93—76 = 17	on -

Objective & strategy	Concrete	Pictorial	Abstract	Y3
Column subtraction without regrouping (friendly numbers)	47—32	Calculations 54 -22 32	47-24=23 -\frac{40+7}{20+4} -\frac{20+3}{20+3}	
	Use base 10 or Numicon to model	Draw representations to support understanding	Intermediate step may be needed to lead to clear subtraction understanding	SL
Column subtraction with regrouping	Tens Units	45 -29 Tens Ones	836-254=582 Begin by partitioning into pv columns.	ubtraction
	Begin with dienes or numicon. Move to pv counters, modelling the exchange of a ten into ten ones. Use the phrase 'take and make' for exchange.	10 + 6 = 16	$728-582=146$ Then move to formal method. $\frac{7}{7} \cdot \frac{12}{2} \cdot \frac{8}{8}$ $\frac{5}{1} \cdot \frac{8}{4} \cdot \frac{2}{6}$	ctio
		Children may draw base ten or PV counters and cross off.		5

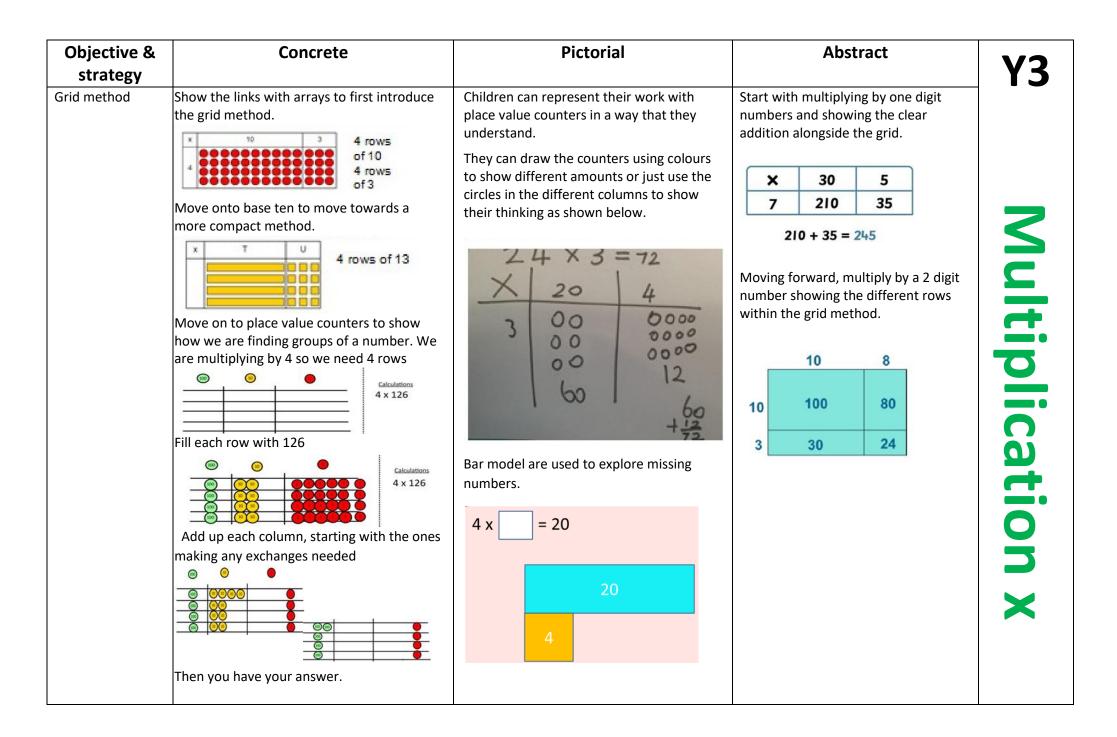
Objective & strategy		Conc	rete	Pictorial	Abstract	Υ
Subtracting tens and ones		234 -	179	Children to draw pv counters and show their exchange—see Y3.	- 6	4 6
Year 4 subtract with	<u></u>	10	•	0	2 7 5 4	4-6
up to 4 digits. Introduce decimal	100 100	10 10 10			-1562	
subtraction through context of money	100	(b) (a) (b) (c) (c) (c) (c) (c) (c) (c) (c) (c) (c			1192	
			hange using then move to PV		Use the phrase 'take and make' for exchange.	nS
Year 5- Subtract with at least 4 digits, including money and measures. Subtract with decimal	As year 4			Children to draw pv counters and show their exchange – see Y3.	2 1 2 8 2 8,9 2 8	ubtractio
values, including mixtures of integers and decimals and aligning the decimal					Use zeros for place holders $7774690000000000000000000000000000000000$	cti
Year 6—Subtract with increasingly large and more complex numbers and decimal values					**************************************	o n -
					- 36 · 08 0 kg 69 · 339 kg	

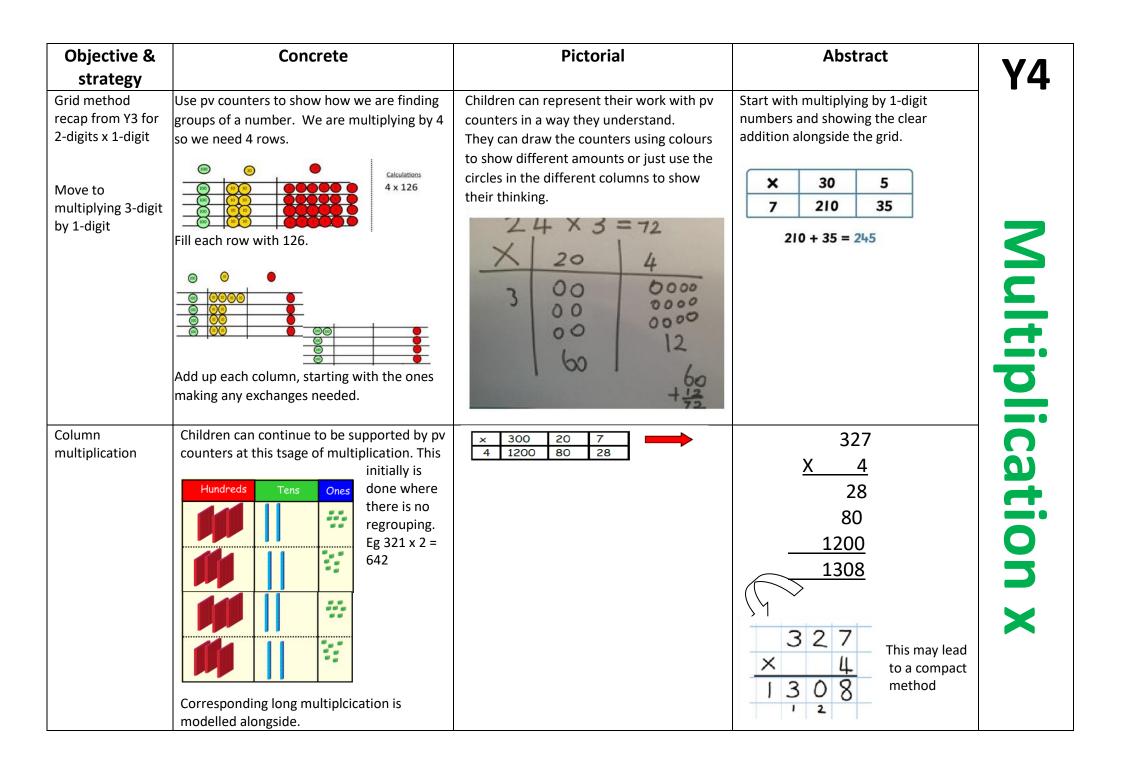
Objective & strategy	Concrete	Pictorial	Abstract	Y1
Doubling	Use practical activities using manipulatives including cubes and numicon to demonstrate doubling.	Double 4 is 8 Draw pictures to show how to double numbers.	16 10 10 10 10 10 10 10 10 10 10 10 10 10	Nul
Counting in multiples	Count the groups as children are skip counting, children may use their fingers as they are skip counting.	Children make representations to show counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30	Multiplicat
Making equal groups and counting the total	Use manipulatives to create equal groups.	Draw to show 2 x 3 = 6 Draw and make representations.	2 x 4 = 8	ation x

Objective & strategy	Concrete	Pictorial	Abstract	Y1
Repeated addition	Use different objects to add equal groups.	There are 3 sweets in one bag. How many sweets are in 5 bags altogether? 3+3+3+3+3 = 15 Use pictorials including number lines to solve problems.	Write addition sentences to describe objects and pictures. 2+2+2+2 = 10	Multiplic
Understanding arrays	Use objects laid out in arrays to find the answers to 2 lots of 5, 3 lots of 2 etc	Draw representations of arrays to show understanding.	3 x 2 = 6 2 x 5 = 10	ication



-	Create arrays using		Y2
6	counters and cubes and numicon.	Use representations of arrays to show different calculations and explore commutativity.	12 = 3 × 4 12 = 4 × 3
	Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does		Use an array to write multiplication sentences and reinforce repeated addition. 00000 00000 5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 5 x 3 = 15 3 x 5 = 15
	not affect the answer.	0000	5+5+5=15 3+3+3+3+3=15 5 x 3 = 15 3 x 5 = 15
Using the Inverse This should be taught alongside division, so pupils learn how they work alongside each other.		8 X	2 x 4 = 8 4 x 2 = 8 8 ÷ 2 = 4 8 ÷ 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 ÷ 4 4 = 8 ÷ 2





Objective & strategy	Concrete	Pictorial	Abstract	Υ
Column multiplication for 3 and 4-digits x 1- digit	Hundreds Tens Ones It is important at this stage that they always multiply the ones first.	x 300 20 7 4 1200 80 28 The grid method may be used to show how this relates to a formal written method.	327 <u>X 4</u> 28 80 1200	5-6
	Children can continue to be supported by pv counters. This initially is done where there is no regrouping eg 321 x 2 = 642	Bar modelling and number lines can also support learners when solving problems with multiplication alongside formal written methods.	1308 3 2 7 X 4 I 3 0 8 This will lead to a compact method	Multip
Column multiplication	Manipulatives may still be used with the corresponding long multiplication modelled alongside.	10 8 8 8 8 8 9 8 9 8 9 9 9 9 9 9 9 9 9 9	1 8 18 x 3 on the 1st row (8x3=24, carrying the 2 for 20, then 1x3) 18 x10 on the 2 nd row. Show multiplying by 10 by putting zero in ones first.	Multiplication x

Objective & strategy	Concrete	Pictorial	Abstract	
Multiplying decimals up to 2 decimal places by a single digit			Remind children that the single digit belongs in the ones column. Line up the decimal points in the question and the answer. 3 · 1 9 × 8 2 5 · 5 2	

Objective & strategy	Concrete	Pictorial	Abstract	Y1
Division as sharing Search Gordons ITP for interactive resources	have 10 cubes, can you share them equally a 2 groups?	Children use pictures or shapes to share quantities. 8 shared between 2 is 4 Sharing: 12 shared between 3 is 4	12 shared between 3 is 4	Y1 Division ÷

Objective & strategy	Concrete	Pictorial	Abstract	Y2
Division as sharing	10	Children use pictures or shapes to share quantities. 8 ÷ 2 = 4	12 ÷ 3 = 4	
	I have 10 cubes, can you share them equally in 2 groups?	Children use bar modelling to show and support understanding. 12 12 ÷ 4 = 3		Divis
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use number lines for grouping. 12 ÷ 3 = 4 Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?	ivision ÷

Objective & strategy	Concrete	Pictorial	Abstract Y3
Division as grouping	Use cubes, counter, objects or pv counters to aid understanding. 24 divided into groups of $6 = 4$ 96 ÷ 3 = 32	Continue to use bar modelling to aid solving division problems. $ 20 $ $? $ $ 20 \div 5 = ? $ $ 5 \times ? = 20 $	How many groups of 6 in 24? 24 ÷ 6 = 4
Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	Draw an array and use lines to split the array into groups to make multiplication and division sentences.	Find the inverse of multiplication and division sentences by creating eight linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7 28 = 7 x 4 28 = 4 x 7 4 = 28 ÷ 7 7 = 28 ÷ 4

Objective & strategy	Concrete	Pictorial	Abstract	Y3
Division with remainders	14 ÷ 3 = Divide objects between groups and see how much is left over	Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder. Draw dots and group them to divide an amount and clearly show a remainder. Use bar models to show division with remainders. 37 10 10 10 10 10 10 10 10 10 1	Complete written divisions and show the remainder using r. 29 ÷ 8 = 3 REMAINDER 5 ↑ ↑ ↑ ↑ dividend divisor quotient remainder	Division +

Objective & strategy	Concrete	Pictorial	Abstract	Υ
Divide at least 3 digit numbers by 1 digit. Short Division	3 2 3 Use place value counters to divide using the bus stop method alongside. 42 ÷ 3= Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over. We exchange this ten for ten ones and then share the ones equally among the groups. We look how much in 1 group so the answer is 14.	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups. Encourage them to move towards counting in multiples to divide more efficiently.	Begin with divisions that divide equally with no remainder. 2 1 8 3 4 8 7 2 Move onto divisions with a remainder. 8 6 r 2 3 5 4 3 2 Finally move into decimal places to divide the total accurately. 1 4 6 16 21 3 5 5 1 1 . 0	4-6 Division -

Long Division

Step 1 – a remainder in the ones

4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).

4 goes into 16 four times.

4 goes into 5 once, leaving a remainder of 1.

8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).

- 8 goes into 32 four times $(3,200 \div 8 = 400)$
- 8 goes into 0 zero times (tens).
- 8 goes into 7 zero times, and leaves a remainder of 7.

When dividing the ones, 4 goes into 7 one time. Multiply $1 \times 4 = 4$, write that four under the 7, and subract. This finds us the remainder of 3.

Check: $4 \times 61 + 3 = 247$

When dividing the ones, 4 goes into 9 two times. Multiply $2 \times 4 = 8$, write that eight under the 9, and subract. This finds us the remainder of 1.

Check: $4 \times 402 + 1 = 1,609$

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o	t o 2	t o 2 9
2)58	2) 5 8 <u>-4</u> 1	2)5 <mark>8</mark> -4 \ 1 <mark>8</mark>
Two goes into 5 two times, or 5 tens ÷ 2 = 2 whole tens but there is a remainder!	To find it, multiply 2 × 2 = 4, write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o 2 <mark>9</mark>	t o 2 9	t o 2 9
2)58 -4 18	2)58 -4 18	2)58 - <u>4</u> 18
	<u>- 1 8</u> 0	<u>- 1 8</u> 0
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The quotient is 29.

Step 2 – a remainder in any of the place values

1. Divide.	2 Multiply 9 publicant	2 Dran dawn the next digit
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
1 2)278	1 2)278 -2 0	18 2)278 -2↓ 07
Two goes into 2 one time, or 2 hundreds ÷ 2 = 1 hundred.	Multiply 1 × 2 = 2, write that 2 under the two, and subtract to find the remainder of zero.	Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
13 2)278 -2 07	13 2)278 -2 07 -6	13 2)278 -2 07 -6 18
Divide 2 into 7. Place 3 into the quotient.	Multiply 3 × 2 = 6, write that 6 under the 7, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
13 <mark>9</mark> 2)278 -2 07 -6 18	139 2)278 -2 07 -6 18 -18	139 2)278 -207 -6 18 -18
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract to find the remainder of zero.	There are no more digits to drop down. The quotient is 139.